

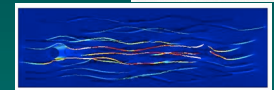
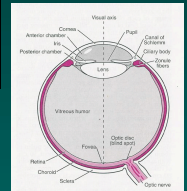
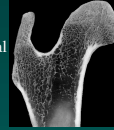
## “Modeling Biomechanical Behavior of Tissues”

Rich Hart  
Department of Biomedical Engineering  
April 4, 2008



## Computational Tissue Mechanics Research Interests

- **Bone Adaptation**  
The ability of living bone to change material properties and geometry in response to mechanical loading. (NIH, past)
- **Ocular Mechanics**  
Understanding the cascade of mechanical events leading to the progressive loss of vision due to glaucoma. (NIH)
- **(New) Multiphysics modeling**  
Modeling motion of cells in gel/cell/fiber composites (NSF pending)  
Modeling motion of cells in flowing blood?



## Software

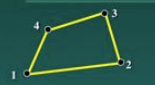
- Finite Element Packages
  - ABAQUS (CalculiX)
  - COMSOL\*
  - RFEM3D (self written)
- Pre- and Postprocessing
  - Patran\*
  - Cubit (Sandia)
- Other
  - MATLAB/Simulink

### Finite Element Method

#### FEM: A Linear Spring Analogy

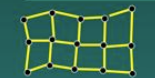


$$\mathbf{F} = \mathbf{k}\mathbf{x}$$



$$\{\mathbf{f}\} = [\mathbf{k}]\{\mathbf{d}\}$$

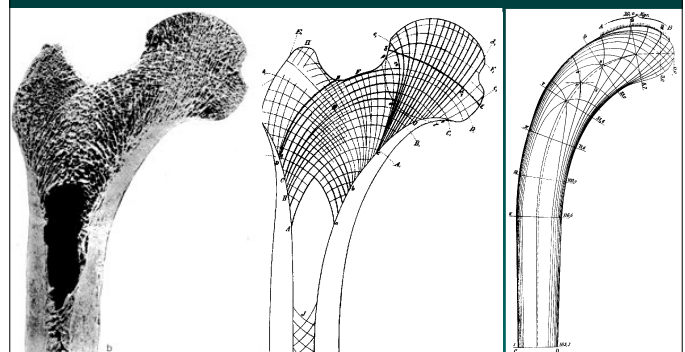
$$[\mathbf{k}] = \int_V [\mathbf{B}]^T [\mathbf{D}] [\mathbf{B}] dV$$



$$\{\mathbf{F}\} = [\mathbf{K}]\{\mathbf{D}\}$$

$$[\mathbf{K}] = \sum_{\text{elements}} [\mathbf{k}]$$

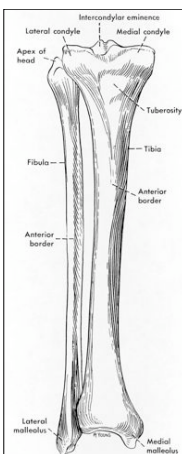
## Wolff's Section and Schematic; Culman's Calculated Stresses (1892)



## Roux's Specimen

A natural “osteotomy experiment”

Cortical shape adaptation:  
“Modeling”

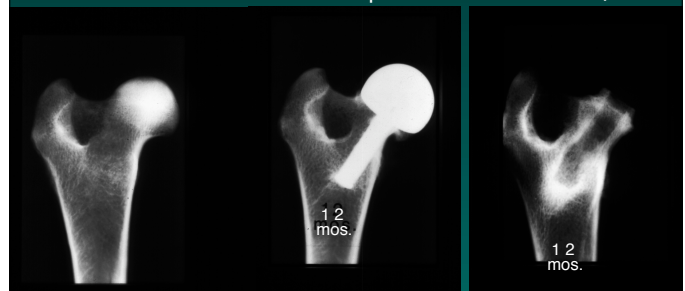


## 1 Year Post-op

Normal

Metal Implant

Carbon composite



Courtesy, Ronald C. Anderson

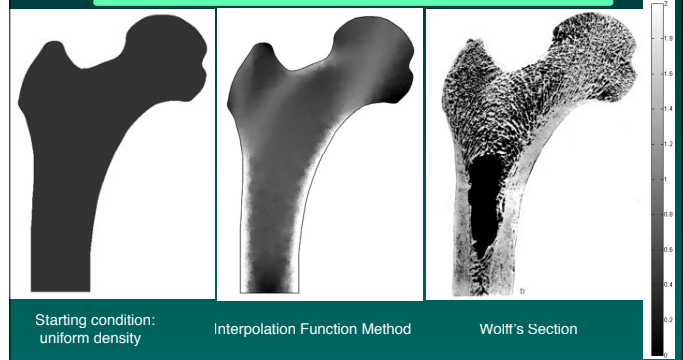
## 'Wolff's Law' (1892)

### 'Bone Form Follows Bone Function'

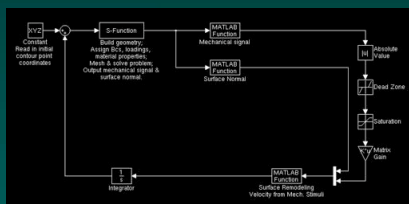
- Trabecular Bone
  - Trabeculae align with the principal stress trajectories (trajectorial theory)
  - Density is related to magnitude of the load
- Cortical Bone
  - Shape depends upon loading

*Can adaptation be modeled, predicted, and manipulated?*

## Evolution of Apparent Density: Form and Function



## Example Application V: Human femur; Daily history

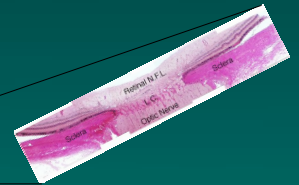
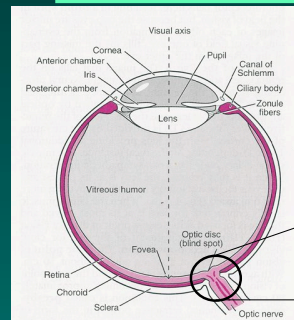


Coupled adaptation in both shape and material properties



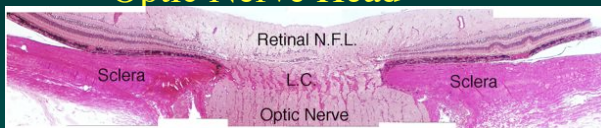
Bone Shape Evolution

## Eye Anatomy



From Rhoades and Tanner, 1995

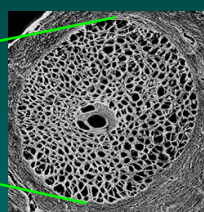
## Optic Nerve Head



Vertical sagittal section of ONH and peripapillary sclera



Transverse view of ONH



SEM of a cross section of the lamina cribrosa network of connective tissues, after all the neural tissues have been removed (trypsin digest).

From Minckler, 1989

## Ocular Mechanics Research: Long Term Goals

### Given:

- Eye Geometry (Optic Nerve Head, ONH)
- Eye Material Properties
- Initial Conditions: Normal pressure
- Altered conditions: Increased pressure

### Predict:

- Progression of damage to supporting tissues of the Optic Nerve Head due to increased pressure
- Loss of support of neural tissues and loss of vision

## Methods – ONH Imaging Apparatus

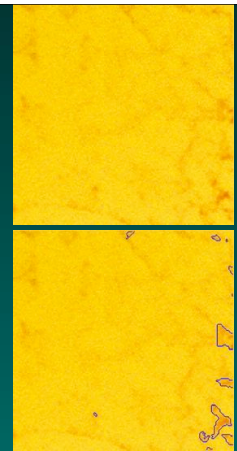
- Designed to obtain serial, transverse images of the stained surface of the embedded tissue within the paraffin block
- Camera magnification is adjusted so that each pixel represents  $2.5 \times 2.5 \mu\text{m}$  of tissue ( $1.5 \times 1.5 \mu\text{m}$ )
- Tissue specimen is mounted on a microtome for  $3 \mu\text{m}$  serial sectioning ( $1.5 \mu\text{m}$ )



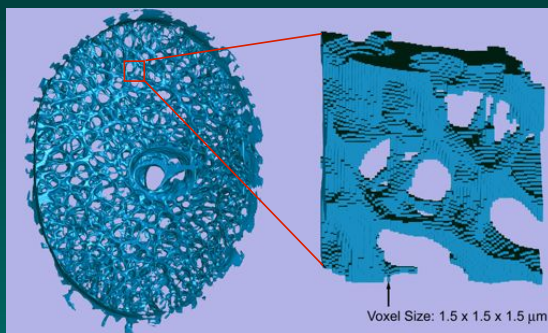
## 3-D Segmentation

- Use 3-D trabecular structure direction to improve the detection and classification of lamina voxels into connective tissue or neural tissue
- Perform Coherence Enhancing Diffusion filtering using the Structure Tensor
- Perform Expectation Maximization incorporating an Anisotropic Markov Random Field
- Within the E-M algorithm, correct for intra- and inter-image illumination differences
- End result is a segmentation of the lamina with remarkable 3-D structural coherence, which is essential for modeling

Grau, Downs, *et al.*, IEEE Medical Imaging, 2006

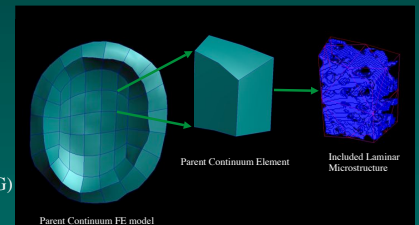


## Laminar Microstructure Varies Regionally



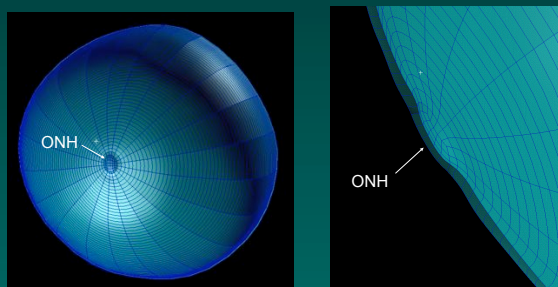
## Modeling Approach

- Generate finite element geometries of the posterior hemisphere, apply IOP loading
- Generate ONH elements large enough to incorporate 5 or more lamina cribrosa beams)
- Query 3-D image database to find the volume fraction and fabric tensor for each finite element.
- Assume that the material properties of an individual beam of the lamina cribrosa are the same as that of the sclera (which can be tested).
- Compare the deformation from experimentally induced pressure increases (20 mmHG) to that calculated for Normal and Glaucomatous eyes.

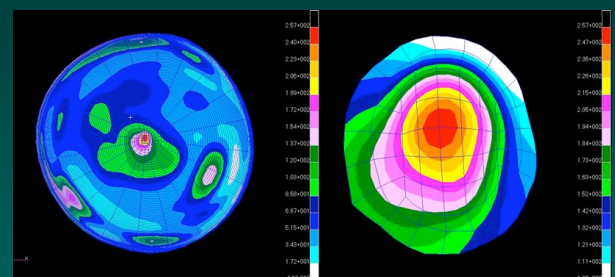


## Individual-specific Model

- Model of individual monkey lamina and peripapillary sclera inserted into a generic scleral shell (anatomic shape and thickness)



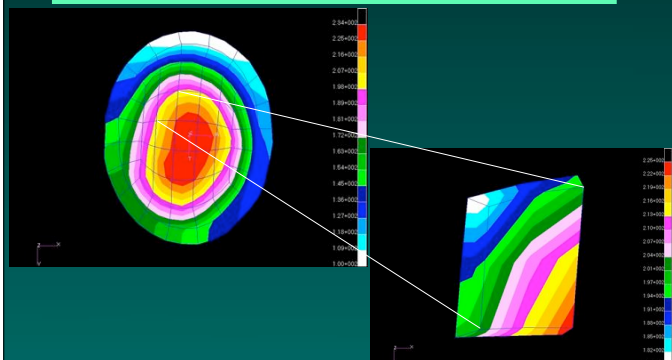
## Results - Displacement ( $\mu\text{m}$ )



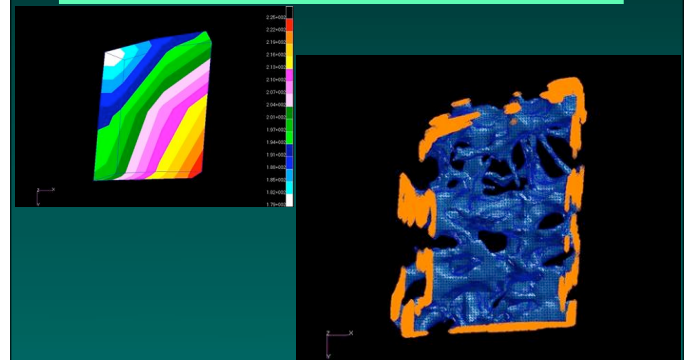
Contour plot showing the magnitude of displacement in an EG eye model



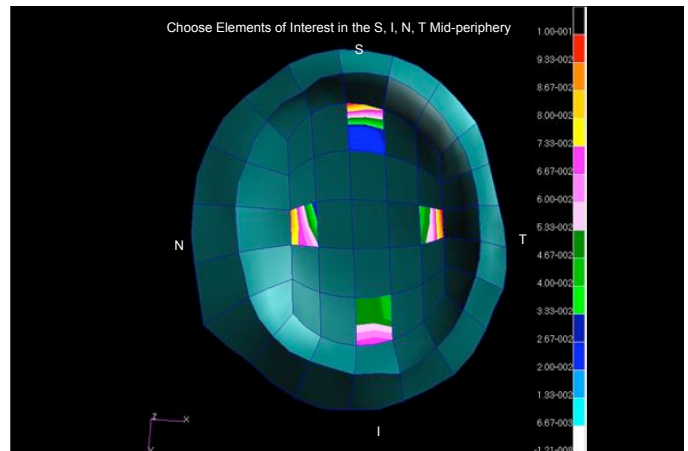
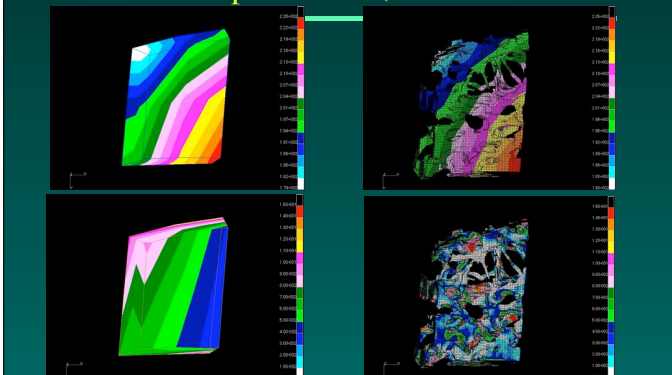
## Results: Continuum Displacements



## Results: Continuum Displacements as Boundary Conditions for MicroModel



## Results: Displacements, Strains

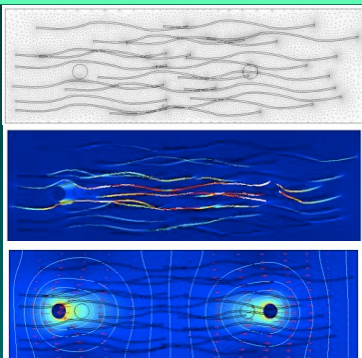


## FEM: Gels, Fibers and Cells

Finite Element  
Mesh

von Mises stress  
carried by fibers

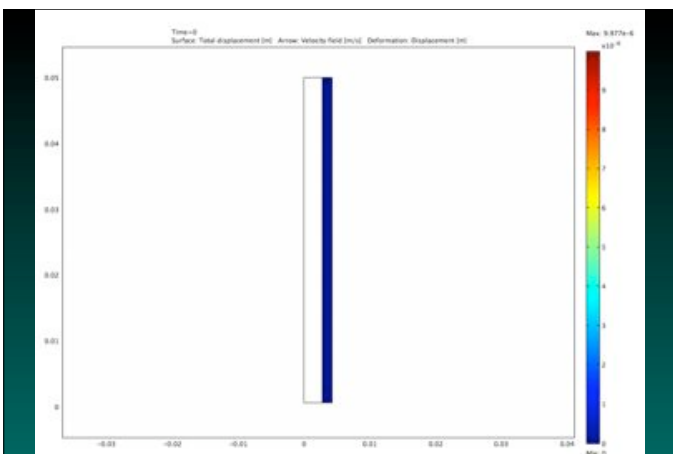
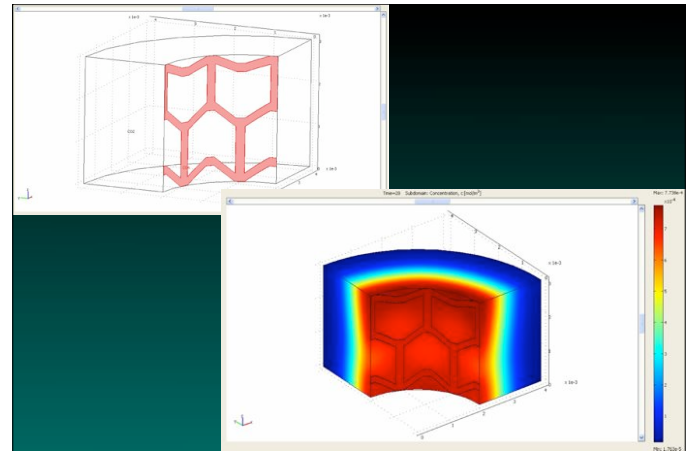
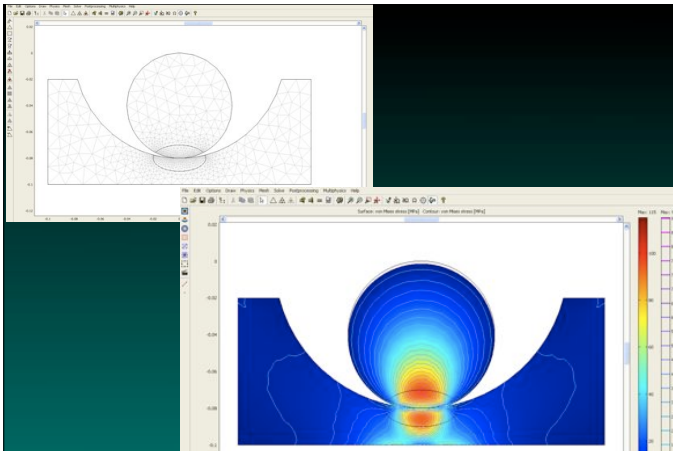
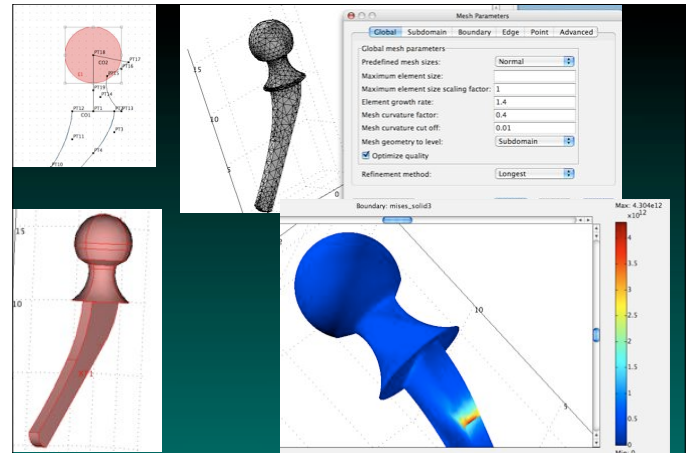
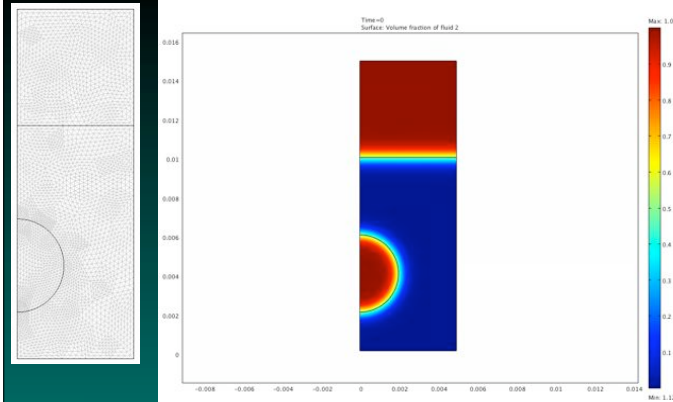
No fibers (properties  
same as gel);  
displacement  
contours shown



## Educational Use

- BME 694 Finite Element Applications in Biomedical Engineering
  - Multiphysics applications
    - Structural
    - Thermal
    - Fluids
    - Diffusion

# COMSOL: Level Set Tutorial



## Acknowledgements

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Thanks for the opportunity  
to present this today!

Questions?

